N40 - Acid Base
$K_{\text {sp }}$

## N40 - Acid Base

Target: I can perform $\mathrm{K}_{\mathrm{sp}}$ calculations to determine the solubility of different salts.

## $\underline{K}_{\underline{p} p}$ Values for Some Salts at $25^{\circ} \mathrm{C}$

| Name | Formula | $\mathrm{K}_{\text {sp }}$ |
| :---: | :---: | :---: |
| Barium carbonate | $\mathrm{BaCO}_{3}$ | $2.6 \times 10^{-9}$ |
| Barium chromate | $\mathrm{BaCrO}_{4}$ | $1.2 \times 10^{-10}$ |
| Barium sulfate | $\mathrm{BaSO}_{4}$ | $1.1 \times 10^{-10}$ |
| Calcium carbonate | $\mathrm{CaCO}_{3}$ | $5.0 \times 10^{-9}$ |
| Calcium oxalate | $\mathrm{CaC}_{2} \mathrm{O}_{4}$ | $2.3 \times 10^{-9}$ |
| Calcium sulfate | $\mathrm{CaSO}_{4}$ | $7.1 \times 10^{-5}$ |
| Copper(I) iodide | CuI | $1.3 \times 10^{-12}$ |
| Copper(II) iodate | $\mathrm{Cu}\left(\mathrm{IO}_{3}\right)_{2}$ | $6.9 \times 10^{-8}$ |
| Copper(II) sulfide | CuS | $6.0 \times 10^{-37}$ |
| Iron(II) hydroxide | $\mathrm{Fe}(\mathrm{OH})_{2}$ | $4.9 \times 10^{-17}$ |
| Iron(II) sulfide | FeS | $6.0 \times 10^{-19}$ |
| Iron(III) hydroxide | $\mathrm{Fe}(\mathrm{OH})_{3}$ | $2.6 \times 10^{-39}$ |
| Lead(II) bromide | $\mathrm{PbBr}_{2}$ | $6.6 \times 10^{-6}$ |
| Lead(II) chloride | $\mathrm{PbCl}_{2}$ | $1.2 \times 10^{-5}$ |
| Lead(II) iodate | $\mathrm{Pb}\left(\mathrm{IO}_{3}\right)_{2}$ | $3.7 \times 10^{-13}$ |
| Lead(II) iodide | $\mathrm{PbI}_{2}$ | $8.5 \times 10^{-9}$ |
| Lead(II) sulfate | $\mathrm{PbSO}_{4}$ | $1.8 \times 10^{-8}$ |


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| Lead(II) sulfate | $\mathrm{PbSO}_{4}$ | $1.8 \times 10^{-8}$ |
| Magnesium carbonate | $\mathrm{MgCO}_{3}$ | $6.8 \times 10^{-6}$ |
| Magnesium hydroxide | $\mathrm{Mg}(\mathrm{OH})_{2}$ | $5.6 \times 10^{-12}$ |
| Silver bromate | $\mathrm{AgBrO}_{3}$ | $5.3 \times 10^{-5}$ |
| Silver bromide | AgBr | $5.4 \times 10^{-13}$ |
| Silver carbonate | $\mathrm{Ag}_{2} \mathrm{CO}_{3}$ | $8.5 \times 10^{-12}$ |
| Silver chloride | AgCl | $1.8 \times 10^{-10}$ |
| Silver chromate | $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$ | $1.1 \times 10^{-12}$ |
| Silver iodate | $\mathrm{AgIO}_{3}$ | $3.2 \times 10^{-8}$ |
| Silver iodide | AgI | $8.5 \times 10^{-17}$ |
| Strontium carbonate | $\mathrm{SrCO}_{3}$ | $5.6 \times 10^{-10}$ |
| Strontium fluoride | $\mathrm{SrF}_{2}$ | $4.3 \times 10^{-9}$ |
| Strontium sulfate | $\mathrm{SrSO}_{4}$ | $3.4 \times 10^{-7}$ |
| Zinc sulfide | ZnS | $2.0 \times 10^{-25}$ |

## Mostly Review!

Equilibrium constants and ICE Tables.
Only real difference is that your reactant is always a solid so it doesn't show up in the Law of Mass Action.

But that isn't "new" - we've known that forever!

## Solubility

We typically describe the solubility in how much solute can you dissolve in how much solvent.

Moles / Liter
Grams / Liter Etc...

Always check what units it wants answers in!
Usually represented by "S"

## Solving Solubility Problems

For the salt Agl at $25^{\circ} \mathrm{C}, \mathrm{K}_{\text {sp }}=1.5 \times 10^{-16}$

$\boldsymbol{K s p}=\left[\mathrm{Ag}^{+}\right]\left[\mathrm{I}^{-}\right]$
Nothing on the denominator because the reactant was a solid!
$1.5 \times 10^{-16}=x^{2}$
$x=$ solubility of Agl in $\mathrm{mol} / \mathrm{L}=1.2 \times 10^{-8} \mathrm{M}$

## Solving Solubility Problems When Not 1:1

For the salt $\mathrm{PbCl}_{2}$ at $25^{\circ} \mathrm{C}, \mathrm{K}_{\text {sp }}=1.6 \times 10^{-5}$ $\mathrm{PbCl}_{2}(\mathrm{~s}) \rightarrow \mathrm{Pb}^{2+}(\mathrm{aq})+2 \mathrm{Cl}-(\mathrm{aq})$

| $I$ | $O$ | $O$ |
| :---: | :---: | :---: |
| $C$ | $+x$ | $+2 x$ |
| $E$ | $x$ | $2 x$ |

Be careful with the stoichiometry!

$$
1.6 \times 10^{-5}=(x)(2 x)^{2}=4 x^{3}
$$

$x=$ solubility of $\mathrm{PbCl}_{2}$ in $\mathrm{mol} / \mathrm{L}=1.6 \times 10^{-2} \mathrm{M}$

## Common Ion Effect

What happens to the solubility of a substance if one of its ions is already present in the solution?

Will the solubility increase or decrease????

## It decreases!

Let's redo this problem but this time let's have some I- already in the solution. $x$ should end up less than $1.2 \times 10^{-8} \mathrm{~mol} / \mathrm{L}$

## Solving Solubility with a Common Ion

For the salt Agl at $25^{\circ} \mathrm{C}, \mathrm{K}_{\text {sp }}=1.5 \times 10^{-16}$ What is its solubility in 0.05 M Nal ?

$$
\begin{aligned}
& 1.5 \times 10^{-16}=(x)(0.05+x) \cong(x)(0.05) \\
& x=\text { solubility of } \mathrm{Agl} \text { in } \mathrm{mol} / \mathrm{L}=3.0 \times 10^{-15} \mathrm{M}
\end{aligned}
$$

The molar solubility of $\mathrm{Pbl}_{2}$ is $1.50 \times 10^{-3} \mathrm{M}$. Calculate the value of $K_{\text {sp }}$ for $\mathrm{PbI}_{2}$.
(A) $3.38 \mathrm{E}^{-9}$

B $4.50 \mathrm{E}^{-6}$
C $1.35 \mathrm{E}^{-8}$
D $1.50 \mathrm{E}^{-3}$
E none of these

The molar solubility of $\mathrm{Pbl}_{2}$ is $1.50 \times 10^{-3} \mathrm{M}$.
Calculate the value of $K_{\text {sp }}$ for $\mathrm{PbI}_{2}$.
(A) $3.38 \mathrm{E}^{-9}$

| $\mathrm{PbI}_{2(\mathrm{~s})}$ | $\leftrightarrow$ | $\mathrm{Pb}^{2+}(\mathrm{aq})$ | + | 2l $^{-}(\mathrm{aq})$ |
| ---: | :---: | :---: | :---: | :---: |
| - | 0 | 0 |  |  |
| - | $+x$ | $+2 x$ |  |  |

$$
\begin{gathered}
K s p=(x)(2 x)^{2} \\
K s p=4(x)^{3} \\
K s p=4\left(1.5 \times 10^{-3}\right)^{3}
\end{gathered}
$$

$$
K s p=1.35 \times 10^{-8}
$$

## Precipitation and Qualitative Analysis

Solution of $\mathrm{Ag}^{+}, \mathrm{Hg}_{2}{ }^{2+}, \mathrm{Pb}^{2+}$

Add cold $\mathrm{HCl}(\mathrm{aq})$

Precipitate of
$\mathrm{AgCl}(\mathrm{s}), \mathrm{Hg}_{2} \mathrm{Cl}_{2}(\mathrm{~s}), \mathrm{PbCl}_{2}(\mathrm{~s})$


## FYI - Complex Ions

Complex ion - a charged species composed of:

1. A metallic cation
2. Ligands

Ligand - Lewis bases that have a lone electron pair that can form a covalent bond with an empty orbital belonging to the metallic cation

## $\mathrm{NH}_{3} \mathbf{C N}^{-}$, and $\mathrm{H}_{2} \mathrm{O}$ are Common Ligands


*NOTE* A lot of Lewis acids/bases act as ligands. They are often involved in solubility problems, which is why we tend to put Ksp in the Acid Base chapter and not always Equilibrium chapter.

## Coordination Number

## Coordination number

## The number of ligands attached to the cation

- 2, 4, and 6 are the most common coordination numbers

| Coordination \# | Example(s) |
| :---: | :--- |
| 2 | $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$ |
| 4 | $\mathrm{CoCl}_{4}{ }^{2-} \quad \mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}$ |
| 6 | $\mathrm{Co}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+} \quad \mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}{ }^{2+}$ |

## Complex Ions and Solubility

$$
\mathrm{AgCl}(s) \leftrightarrows \mathrm{Ag}^{+}+\mathrm{Cl}^{-} \quad \mathrm{K}_{\mathrm{sp}}=1.6 \times 10^{-10}
$$

$$
\mathrm{Ag}^{\prime}+\mathrm{NH}_{3} \leftrightarrows \mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+} \quad \mathrm{K}_{1}=2.1 \times 10^{3}
$$

$\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+} \mathrm{NH}_{3} \leftrightarrows \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+} \quad \mathrm{K}_{2}=8.2 \times 10^{3}$
$\mathrm{AgCl}+2 \mathrm{NH}_{3} \leftrightarrows \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}+\mathrm{Cl}^{-} \quad \mathrm{K}=\mathrm{K}_{\mathrm{sp}} \cdot \mathrm{K}_{1} \cdot \mathrm{~K}_{2}$

$$
K=2.8 \times 10^{-3}=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}\right]\left[\mathrm{Cl}^{-}\right]}{\left[\mathrm{NH}_{3}\right]^{2}}
$$

## Practice to Glue In

[14] When solid $\mathrm{BaF}_{2}$ is added to $\mathrm{H}_{2} \mathrm{O}$ the following equilibrium is established.

$$
\mathrm{BaF}_{2}(\mathrm{~s}) \rightleftharpoons \mathrm{Ba}^{2+}(\mathrm{aq})+2 \mathrm{~F}^{-}(\mathrm{aq}) \quad K_{\mathrm{sp}}=1.5 \times 10^{-6} \text { at } 25^{\circ} \mathrm{C}
$$

a. Calculate the molar solubility of barium fluoride at $25^{\circ} \mathrm{C}$.
b. Explain how adding each of the following substances affects the solubility of $\mathrm{BaF}_{2}$ in water.
i. $0.10 \mathrm{M} \mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$
ii. $0.10 \mathrm{M} \mathrm{HNO}_{3}$
c. In an experiment to determine the $K_{\text {sp }}$ of $\mathrm{PbF}_{2}$ a student starts with $0.10 \mathrm{M} \mathrm{Pb}\left(\mathrm{NO}_{3}\right)_{2}$ and 0.10 M KF and uses the method of serial dilutions to find the lowest $\left[\mathrm{Pb}^{2+}\right]$ and $\left[\mathrm{F}^{-}\right]$that form a precipitate when mixed. If the student uses the concentration of the ions in the combined solution to determine $K_{\text {sp }}$, will the value of $K_{\text {sp }}$ calculated be too large, too small or just right? Explain.
$K_{\text {sp }}$ for $\mathrm{PbF}_{2}=4.0 \times 10^{-8}$
d. i. In a solution of 0.010 M barium nitrate and 0.010 M lead(II) nitrate, which will precipitate first, $\mathrm{BaF}_{2}$ or $\mathrm{PbF}_{2}$, as $\mathrm{NaF}(\mathrm{s})$ is added? Assume volume changes are negligible. Explain (support your answer with calculations).
ii. When the more soluble fluoride begins to precipitate, what is the concentration of the cation for the less soluble fluoride that remains in solution?

## Key

a. If $S=$ molar solubility of $\mathrm{BaF}_{2}(\mathrm{~s})$, then $\left[\mathrm{Ba}^{2+}\right]=S,[\mathrm{~F}]=2 S$
$\mathrm{K}_{\mathrm{sp}}=\left[\mathrm{Ba}^{2+}\right][\mathrm{F}]^{2}=(S)(2 S)^{2}=4 S^{3}=1.5 \times 10^{-6}$
$S=0.00721 \mathrm{~mol} / \mathrm{L}$
b. i. Adding $\mathrm{Ba}^{2+}$ ion will decrease the molar solubility of $\mathrm{BaF}_{2}$ due to the common ion effect.
ii. Adding $\mathrm{H}^{+}$will increase the molar solubility of $\mathrm{BaF}_{2}$ as the $\mathrm{F}^{-}$ion will react with $\mathrm{H}^{+}$to form HF , thereby causing more $\mathrm{BaF}_{2}$ to dissolve by Le Chatelier's Principle.
c. The calculated $\mathrm{K}_{\mathrm{sp}}$ will be too large because the student is relying on seeing the formation of a precipitate at the moment that Q exceeds $\mathrm{K}_{\mathrm{sp}}$. The student will miss the exact moment that happens, so the calculated value of $\mathrm{K}_{\mathrm{sp}}$ will be too large.
Other possible issues: Protolysis will decrease the concentration of fluoride, so more fluoride will need to be added to cause precipitation; therefore measured $\mathrm{K}_{\text {sp }}$ will be too large. Likewise, some complex ions such as $\mathrm{PbF}^{+}$or $\mathrm{PbF}_{2}(\mathrm{aq})$ may form, again leading to an experimental value that is too large.

## Key

d. i. As both $\mathrm{BaF}_{2}$ and $\mathrm{PbF}_{2}$ are 1:2 compounds, and the concentrations of the metal ions are both 0.010 M , you can tell that $\mathrm{PbF}_{2}$ will precipitate first, because it has the lower $\mathrm{K}_{\mathrm{sp}}$. For calculations to support this: For $\mathrm{PbF}_{2}, \quad 4.0 \times 10^{-8}=(0.01)[\mathrm{F}]^{2} \quad[\mathrm{~F}]^{2}=4.0 \times 10^{-6} \quad[\mathrm{~F}]=2.0 \times 10^{-3} \mathrm{M}$ For $\mathrm{BaF}_{2}, \quad 1.5 \times 10^{-6}=(0.01)\left[\mathrm{F}^{-}\right]^{2} \quad\left[\mathrm{~F}^{-}\right]^{2}=1.5 \times 10^{-4} \quad\left[\mathrm{~F}^{-}\right]=1.2 \times 10^{-2} \mathrm{M}$ The $\mathrm{PbF}_{2}$ will precipitate first because a lower value for the concentration of fluoride is needed.
ii. From part (i) we know that the $\mathrm{BaF}_{2}$ precipitates second, when the [ F$]$ reaches $1.2 \times 10^{-2} \mathrm{M}$

Since $\mathrm{PbF}_{2}$ (s) is present, then $\left[\mathrm{Pb}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}=K_{\text {sp }}=4.0 \times 10^{-8}$

$$
\begin{aligned}
& {\left[\mathrm{Pb}^{2+}\right]\left(1.2 \times 10^{-2}\right)^{2}=4.0 \times 10^{-8}} \\
& {\left[\mathrm{~Pb}^{2+}\right]=2.8 \times 10^{-4} \mathrm{M}}
\end{aligned}
$$

## YouTube Link to Presentation

WWW.

